

Unsupervised Motion Representation Learning with Capsule Autoencoders



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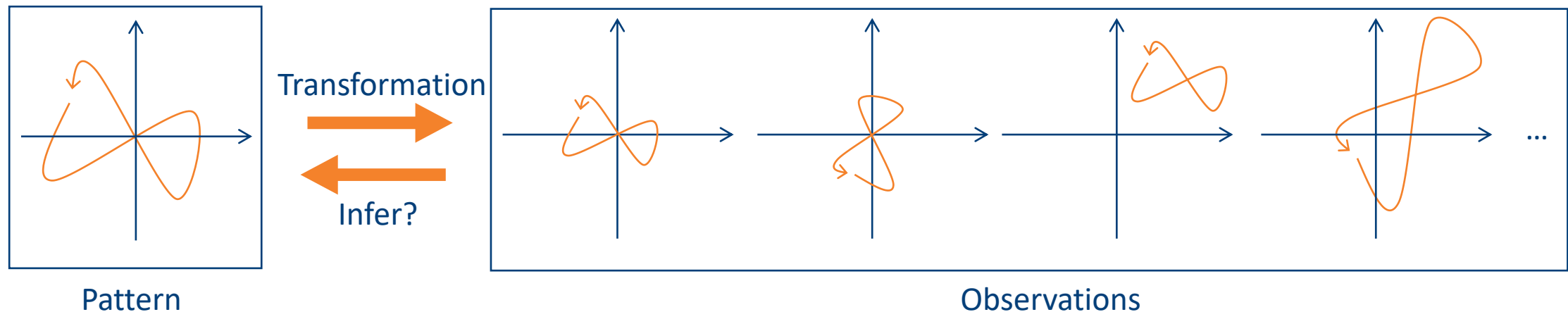


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Problem Formulation

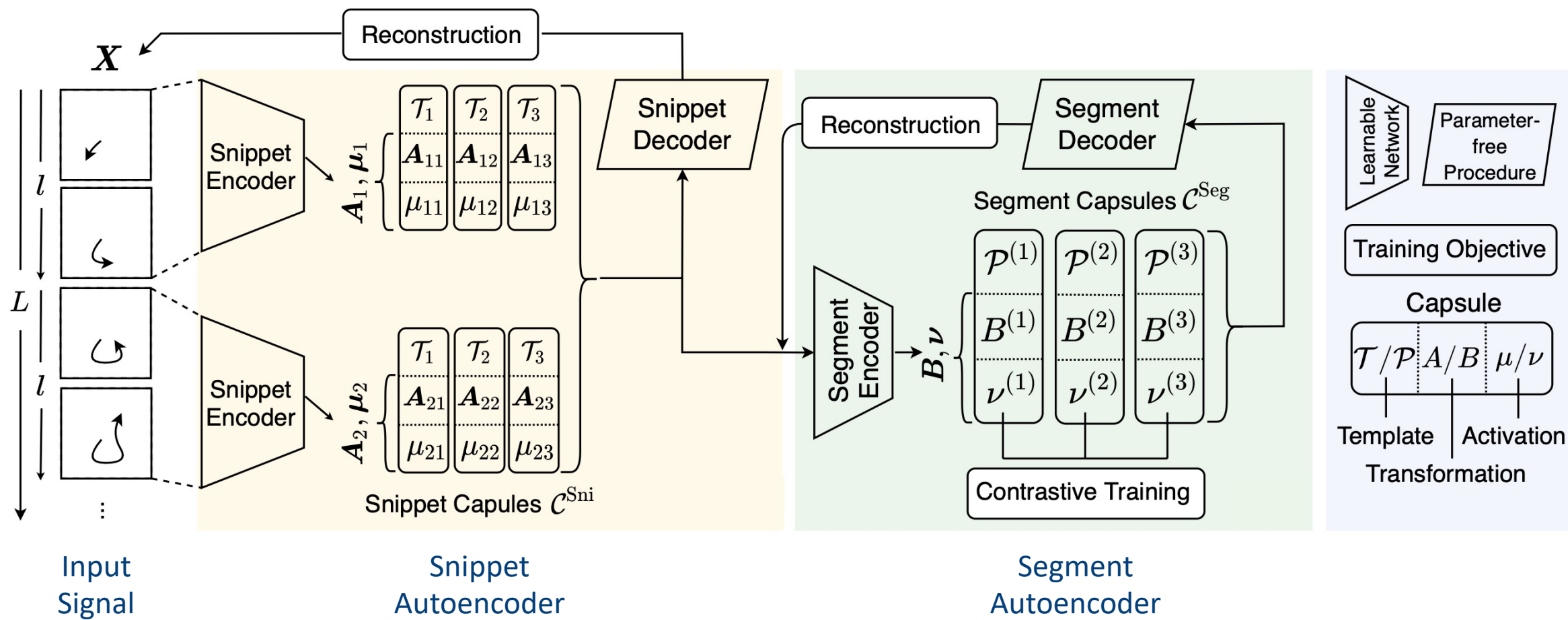
- A trajectory described as $X = \{x_i | i = 1, \dots, L\}, x_i \in \mathbb{R}^d$
- The trajectory belongs to one motion pattern
 - Subject to an arbitrary and unknown transformation
- Given sufficient X s, can we infer their patterns without supervision?
 - Key: separation of identity and transformation



- Framework
- Snippet Autoencoder
- Segment Autoencoder
- Training

Method – Framework

MCAE: Motion Capsule Autoencoder



Method – Snippet Autoencoder

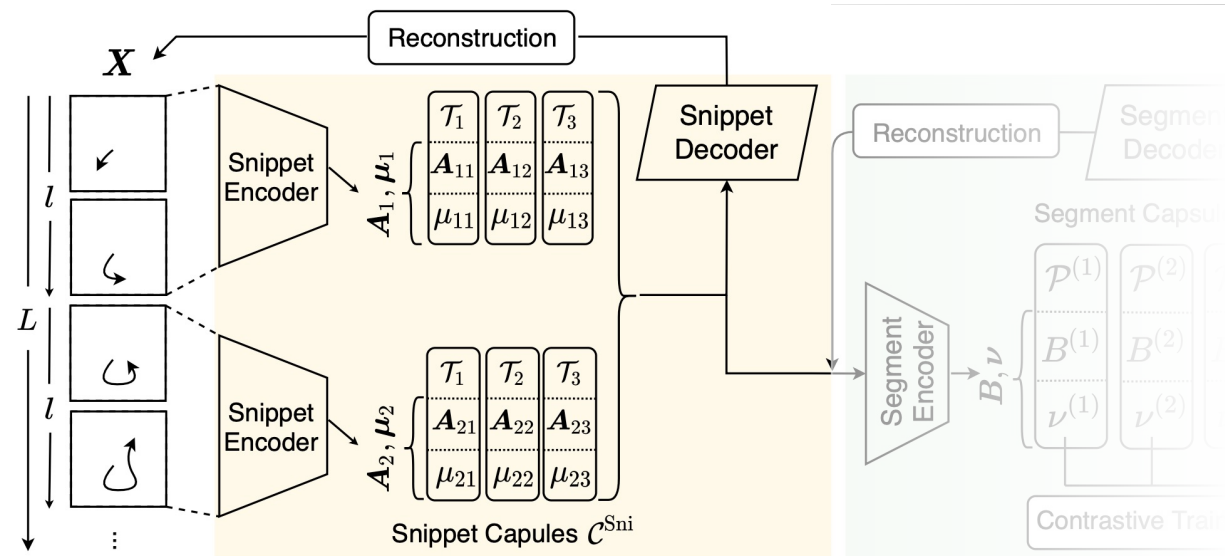
- SniCap = trainable template \mathcal{T} + data-dependent parameters (A, μ)
- Divide input X into l -long snippets
- For each snippet, a snippet encoder predicts (A, μ)
- (A, μ) + template \mathcal{T} : reconstructs input snippets

Decoding:

$$\mathcal{T} = \{t_i | t_i \in \mathbb{R}^d, i = 1, \dots, l\}$$

$$\begin{pmatrix} \hat{t}_{ij} \\ 1 \end{pmatrix} = A_i \begin{pmatrix} t_j \\ 1 \end{pmatrix}, \quad i = 1, \dots, N, \quad j = 1, \dots, l$$

$$\hat{x}_j = \sum_{i=1}^N \mu_i \hat{t}_{ij}, \quad j = 1, \dots, l$$



Method – Segment Autoencoder

- SegCap = trainable template \mathcal{P} + data-dependent parameters (B, ν)
- Template \mathcal{P} defines the relation between a SegCap and \mathcal{T}
- For input snippet parameters, a segment encoder predicts (B, ν)
- $(B, \nu) + \mathcal{P}$: reconstructs input snippet parameters

Encoding:

$$\mathbf{h} = f_{\text{LSTM}}\left(\left[\mathcal{C}_1^{\text{Sni}}, \dots, \mathcal{C}_S^{\text{Sni}}\right]\right),$$

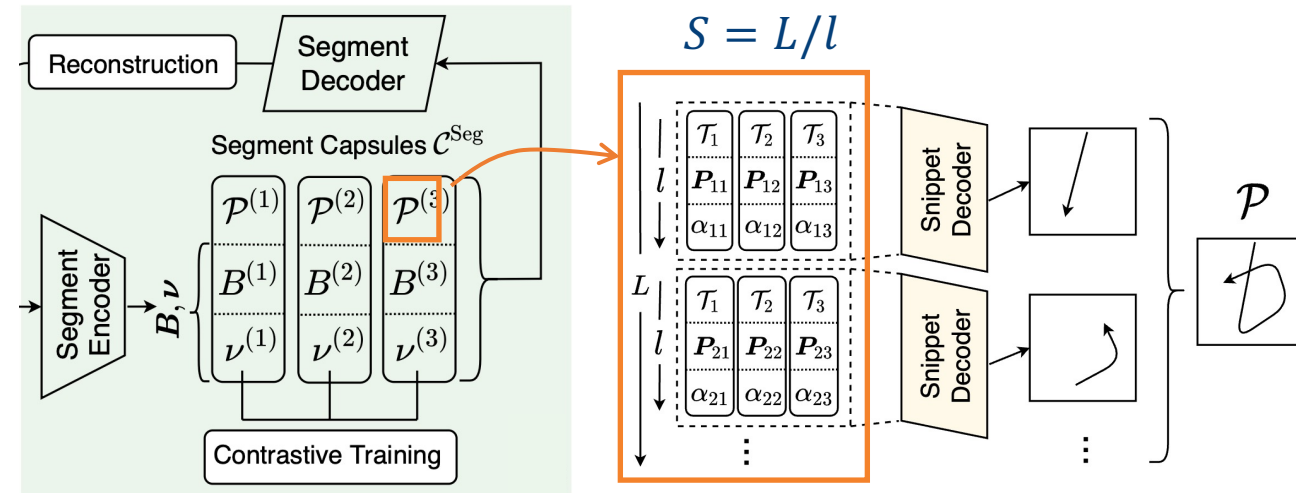
$$\{\mathbf{B}^{(k)}, \nu^{(k)}\} = f_{\text{FC}}^{(k)}(\mathbf{T}, \mathbf{h}), \quad k = 1, \dots, M,$$

Concatenated snippet templates

Decoding:

$$\hat{\mathbf{P}}_{ij}^{(k)} = \mathbf{B}^{(k)} \times \mathbf{P}_{ij}^{(k)}, \quad i = 1, \dots, S, \quad j = 1, \dots, N, \quad k = 1, \dots, M,$$

$$\hat{\mathcal{C}}_i^{\text{Sni}} = (\hat{\mathbf{A}}_i, \hat{\boldsymbol{\mu}}_i) = \left(\sum_{k=1}^M \nu^{(k)} \hat{\mathbf{P}}_i^{(k)}, \sum_{k=1}^M \nu^{(k)} \boldsymbol{\alpha}_i^{(k)} \right), \quad i = 1, \dots, S,$$



- Framework
- Snippet Autoencoder
- Segment Autoencoder
- Training

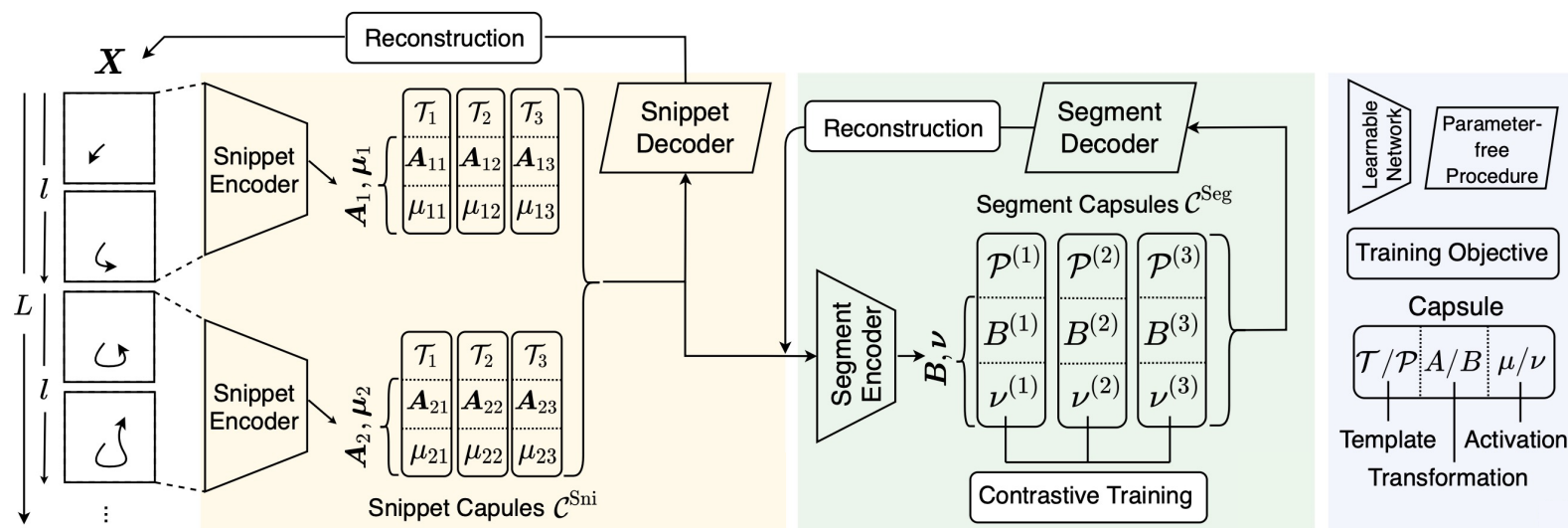
Method – Training

$$\mathcal{L} = \lambda^{\text{Sni}} \mathcal{L}_{\text{Rec}}^{\text{Sni}} + \lambda^{\text{Seg}} \mathcal{L}_{\text{Rec}}^{\text{Seg}} + \mathcal{L}_{\text{Con}}^{\text{Seg}} + 0.5 \mathcal{L}_{\text{Smt}}^{\text{Reg}} + 0.05 \mathcal{L}_{\text{Sps}}^{\text{Reg}}$$

$$\mathcal{L}_{\text{Smt}}^{\text{Reg}} = \sum_{i=2}^L \|\hat{\mathbf{x}}_i - \hat{\mathbf{x}}_{i-1}\|_2^2$$

$$\mathcal{L}_{\text{Rec}}^{\text{Sni}} = \sum_{i=1}^L \|(\hat{\mathbf{x}}_i - \mathbf{x}_i)\|_2^2$$

$$\mathcal{L}_{\text{Rec}}^{\text{Seg}} = \sum_{i=1}^S \|(\hat{\mathbf{A}}_i - \mathbf{A}_i)\|_2^2 + \|(\hat{\boldsymbol{\mu}}_i - \boldsymbol{\mu}_i)\|_2^2$$



$$\mathcal{L}_{\text{Con}}^{\text{Seg}} = -\frac{1}{B} \sum_{i=1}^B \log \frac{\exp(\text{cossim}(\nu'_i, \nu''_i)/\tau)}{\sum_{j=1}^B \exp(\text{cossim}(\nu'_i, \nu''_j)/\tau)}$$

$$\mathcal{L}_{\text{Sps}}^{\text{Reg}} = \|\nu\|_2^2$$

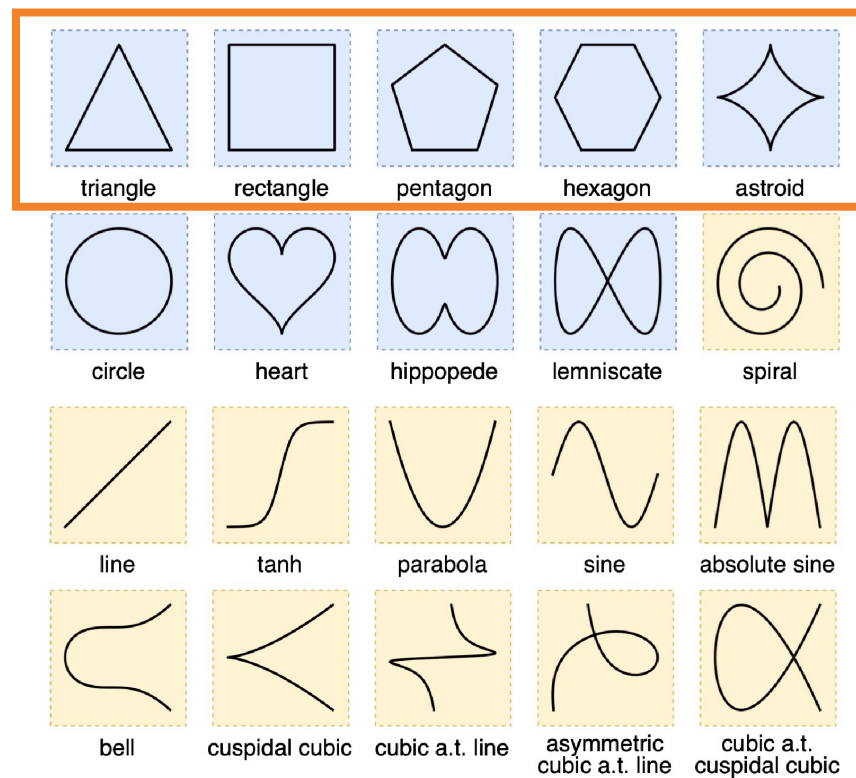
Experiment

- Questions to answer:
 - What are the effects of hyperparameters?
 - How effective and efficient is MCAE?
 - What does MCAE learn?
 - Does MCAE work well for real-world systems?
- Datasets:
 - Trajectory20
 - NWUCLA, NTU-RGBD 60/120

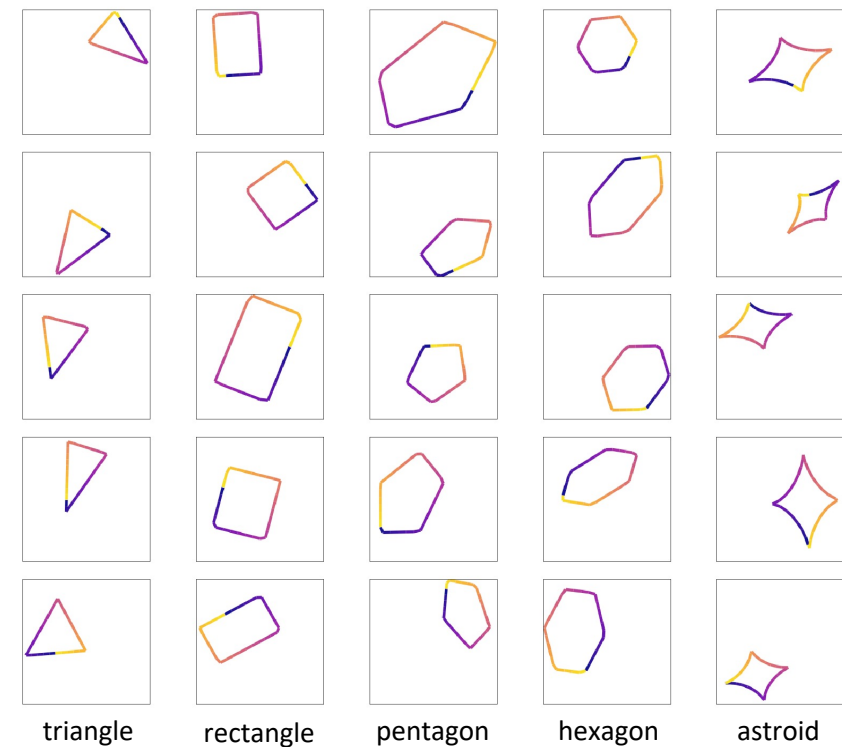
Experiment – Datasets (1)

■ Trajectory20 (T20)

- Twenty motion patterns in 2D space spanning 32 timesteps
- Transformation: rotation, scaling, translation, initial and end points

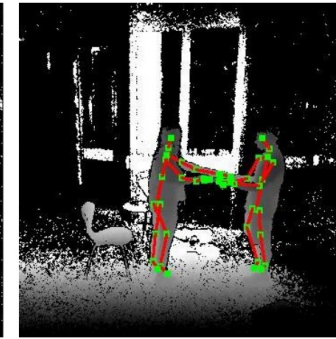
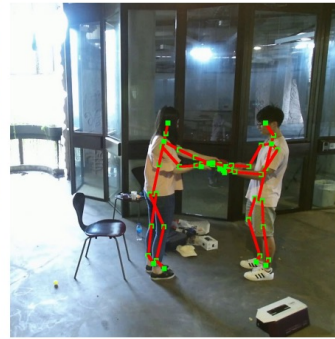
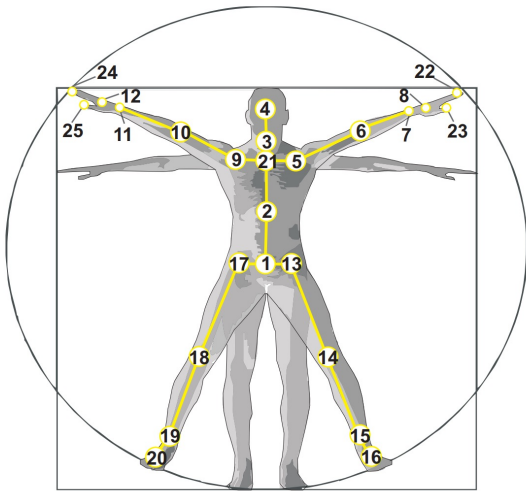


Transformation



Experiment – Datasets (2)

- Skeleton-based action recognition datasets:
 - NW-UCLA, NTU-RGBD 60/120
 - Multi-point motion system in 3D space



Experiment – Learning Motion on T20

- On Trajectory20:
 - What are the effects of hyperparameters?
 - How effective and efficient is MCAE?
 - What does MCAE learn?
- On NW-UCLA and NTU-RGBD 60/120
 - Does MCAE work well for multi-point real-world systems?

Table 1: Ablation study on T20.

Reg.	l	#Sni	#Seg	Acc. (%)
Full	8	8	80	69.30 \pm 0.76
	4	8	80	41.01 \pm 8.81
	16	8	80	45.83 \pm 8.36
	8	2	80	64.02 \pm 2.10
	8	4	80	68.17 \pm 0.36
	8	16	80	48.11 \pm 1.60
	8	8	32	42.36 \pm 3.15
	8	8	64	63.94 \pm 1.41
	8	8	128	69.44 \pm 1.69
w/o $\mathcal{L}_{\text{Smt}}^{\text{Reg}}$	8	8	80	67.60 \pm 1.69
w/o $\mathcal{L}_{\text{Sps}}^{\text{Reg}}$	8	8	80	65.92 \pm 1.63

l : length of snippets

#Sni: number of snippet capsules

#Seg: number of segment capsules

Table 2: Unsupervised learning performance of MCAE and baselines on T20.

	Hidden Param.	#Param.	Acc. (%)
KMeans	–	–	8.57 \pm 0.04
DTW-KMeans	–	–	9.12 \pm 0.20
k -Shape [31]	–	–	12.94 \pm 0.34
LSTM	128	600k	29.17 \pm 2.45
	256	669k	40.03 \pm 0.57
	512	805k	45.59 \pm 1.37
	1,024	1,078k	53.47 \pm 1.52
	2,048	1,625k	54.32 \pm 0.55
1D-Conv	128	588k	44.78 \pm 0.57
	256	787k	53.69 \pm 0.53
	512	1,185k	57.57 \pm 0.56
	1,024	1,982k	57.58 \pm 0.08
	(#Sni, #Seg)	#Param.	Acc. (%)
MCAE	(8, 80)	277k	69.30 \pm 0.76

- What are the effects of hyperparameters?
- How effective and efficient is MCAE?
- What does MCAE learn?
- On NW-UCLA and NTU-RGBD 60/120
 - Does MCAE work well for multi-point real-world systems?

Experiment – Look into Capsules (1)

- Visualization of snippet/segment templates
 - Snippet templates: lines and “hooks”
 - Segment templates: higher resemblance with patterns in T20

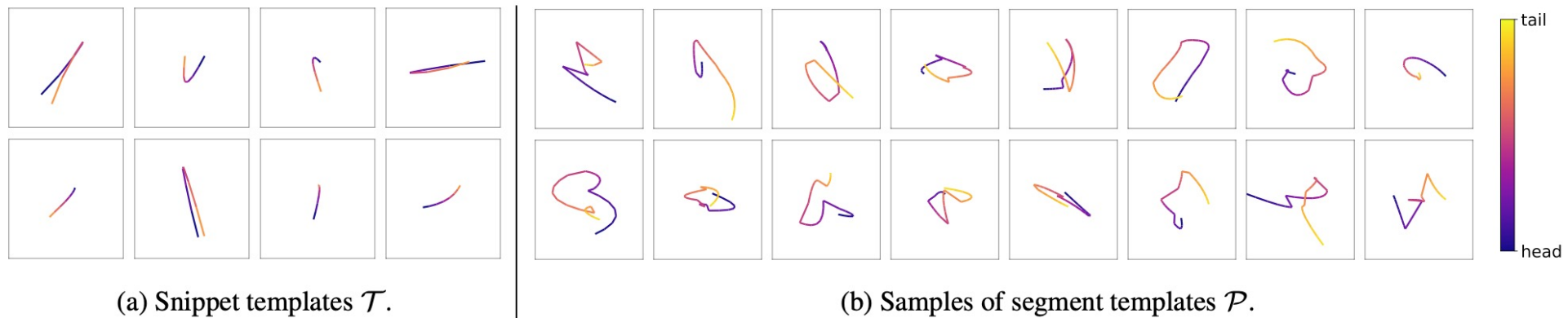




Figure 4: Templates learned from Trajectory20 dataset. Color indicates time.

Experiment – Look into Capsules (2)

- Changes of segment parameters in response to input perturbation
 - Translate input by $(\Delta x, \Delta y)$
 - Check the translation component of segment parameters B .

Table 5: Top-5 segment templates (sorted by segment activation ν then segment ID for better visualization), and the translation (x, y) calculated from their parameters B .

Input	$(\Delta x, \Delta y) = (-0.2, 0)$			$(\Delta x, \Delta y) = (-0.1, 0)$			$(\Delta x, \Delta y) = (0, 0)$			$(\Delta x, \Delta y) = (0, 0.1)$			$(\Delta x, \Delta y) = (0, 0.2)$		
	ID	x	y	ID	x	y	ID	x	y	ID	x	y	ID	x	y
	2	0.05	0.18	2	0.17	0.19	2	0.27	0.19	2	0.28	0.28	2	0.27	0.37
	8	0.01	-0.07	8	0.09	-0.06	8	0.18	-0.04	8	0.19	0.04	8	0.19	0.12
	12	-0.09	0.13	12	0.00	0.13	12	0.09	0.13	12	0.09	0.23	12	0.09	0.32
	37	0.10	-0.11	37	0.18	-0.11	37	0.27	-0.11	37	0.27	-0.03	37	0.27	0.05
	66	-0.12	0.16	66	-0.03	0.16	66	0.05	0.17	66	0.06	0.26	66	0.06	0.35
	2	0.04	0.2	2	0.14	0.19	2	0.24	0.19	2	0.24	0.28	2	0.23	0.38
	5	-0.01	0.30	5	0.07	0.29	5	0.16	0.29	5	0.16	0.38	5	0.15	0.46
	7	0.20	-0.16	7	0.28	-0.16	7	0.37	-0.15	7	0.36	-0.06	7	0.36	0.04
	37	0.04	-0.17	37	0.12	-0.16	37	0.21	-0.16	37	0.20	-0.07	37	0.20	0.01
	46	0.02	0.01	46	0.13	0.02	46	0.23	0.04	46	0.23	0.13	46	0.22	0.23

Experiment – Skeleton Actions

- MCAE -> MCAE-MP
- Multiple joints: encoded independently, use concatenated representation
- 3D trajectory: projected to three orthogonal 2D planes

Table 3: Performance (%) for skeleton-based action classification. Column “Mod.” shows the data modality, where “S” indicates skeleton and “D” indicates depth map. Column “Cls.” shows the auxiliary classifier used for supervised training. We also report supervised SOTAs for completeness.

	Model	Mod.	Cls.	NTU60		NTU120		NW-UCLA
				XSUB	XVIEW	XSUB	XSET	V1&V2 → V3
Unsupervised	Luo <i>et al.</i> [27]	S+D	SLP	61.4	53.2	–	–	50.7
	Li <i>et al.</i> [20]	S+D	SLP	68.1	63.9	–	–	62.5
	SeBiReNet [29]	S	LSTM	–	79.7	–	–	80.3
	LongT GAN [63]	S	SLP	39.1	48.1	–	–	74.3
	MS ² L [24]	S	SLP	52.6	–	–	–	76.8
	CAE+ [33]	S	SLP	58.5	64.8	48.6	49.2	–
	MCAE-MP (SLP)	S	SLP	65.6	74.7	52.8	54.7	83.6
	P&C [41]	S	1-NN	50.7	76.1	–	–	84.9
	MCAE-MP (1-NN)	S	1-NN	51.9	82.4	42.3	46.1	79.1
Supv.	DropGraph [2]	S	–	90.5	96.6	82.4	84.3	93.8
	JOLO-GCN [1]	S	–	93.8	98.1	87.6	89.7	–

Conclusion

- MCAE learns representation for motion that is
 - Discriminative: segment activation reveals semantic information
 - Efficient: requires significantly less parameters compared with baselines
 - Robust against transformation
- Works well on both synthetic and real-world scenarios
- MCAE can be helpful in other sequence analysis tasks
 - Joint modeling of visual appearance and motion in video
 - As mid-level feature in other models (e.g., GCN) for tasks beyond classification

Thank you!

- See you in the poster session...
- Source code and Trajectory20 📌



<https://github.com/ZiweiXU/CapsuleMotion>